

# ***A CGC Monte-Carlo Event Generator For forward hadron productions***

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ArXiv:hep-ph1410.2018

- Introduction
- Monte-Carlo kt-factorization approach
- Event generator version of DHJ formula
- Transverse momentum spectra at RHIC and LHC
- Summary

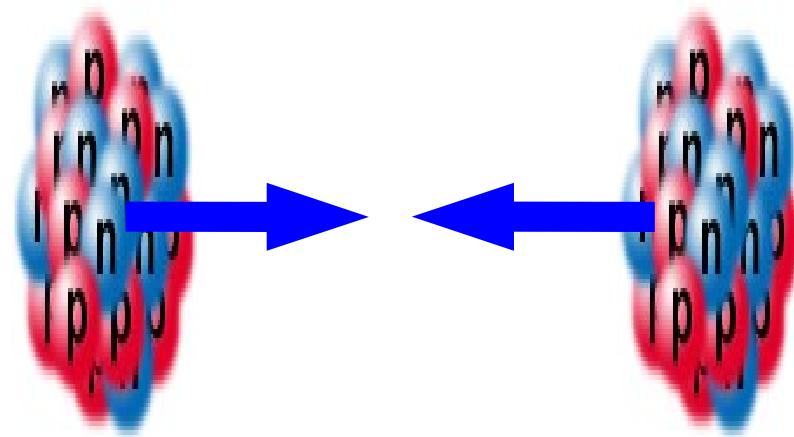
# RHIC and LHC

The 3.8 km circumference

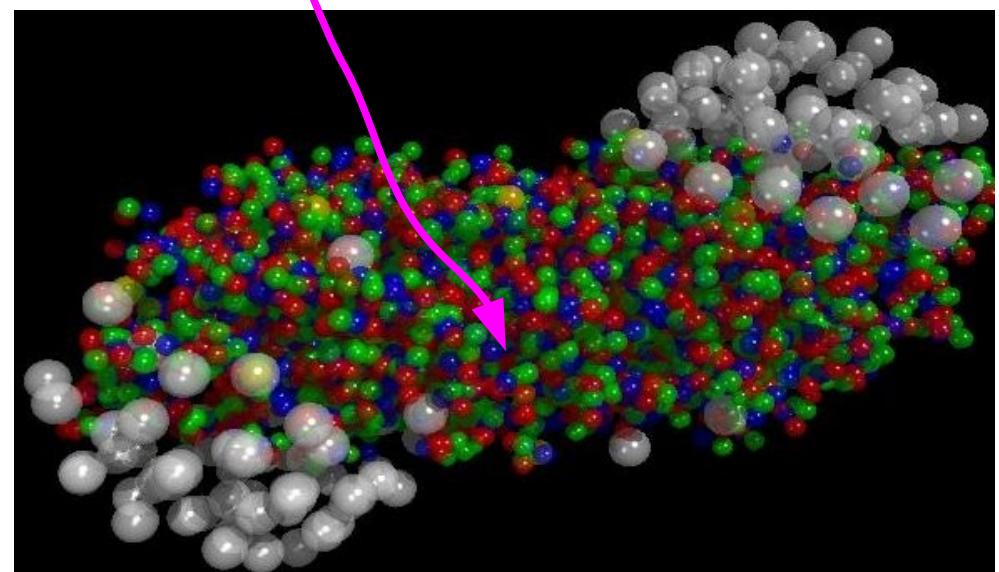


RHIC: Au+Au at C.M. Energy  
of 200GeV per nucleon.

LHC: Pb+Pb at C.M. Energy  
of 2.76TeV per nucleon.



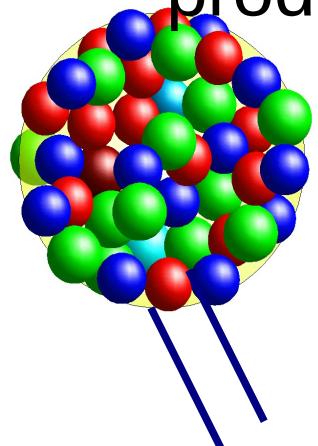
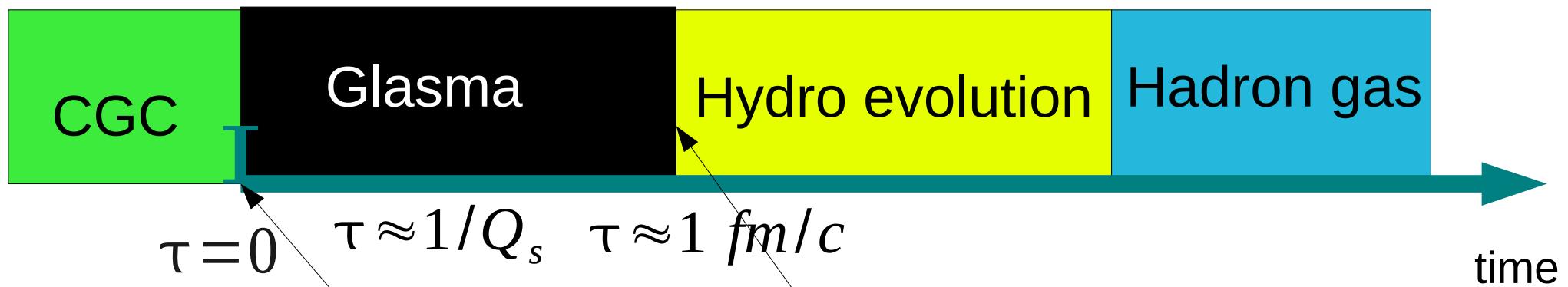
**Creation of Hot and dense matter.**



# High energy heavy ion collisions

Initial state interactions

Final state interactions



$$r \sim \frac{1}{Q_s}$$

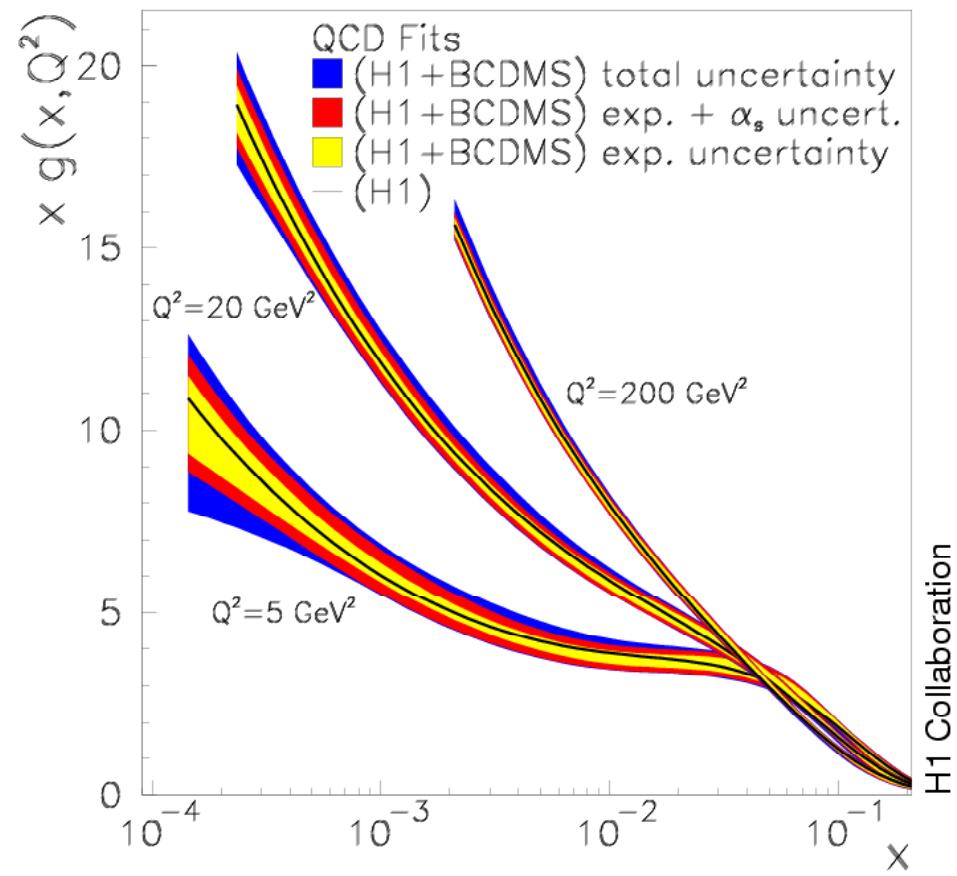
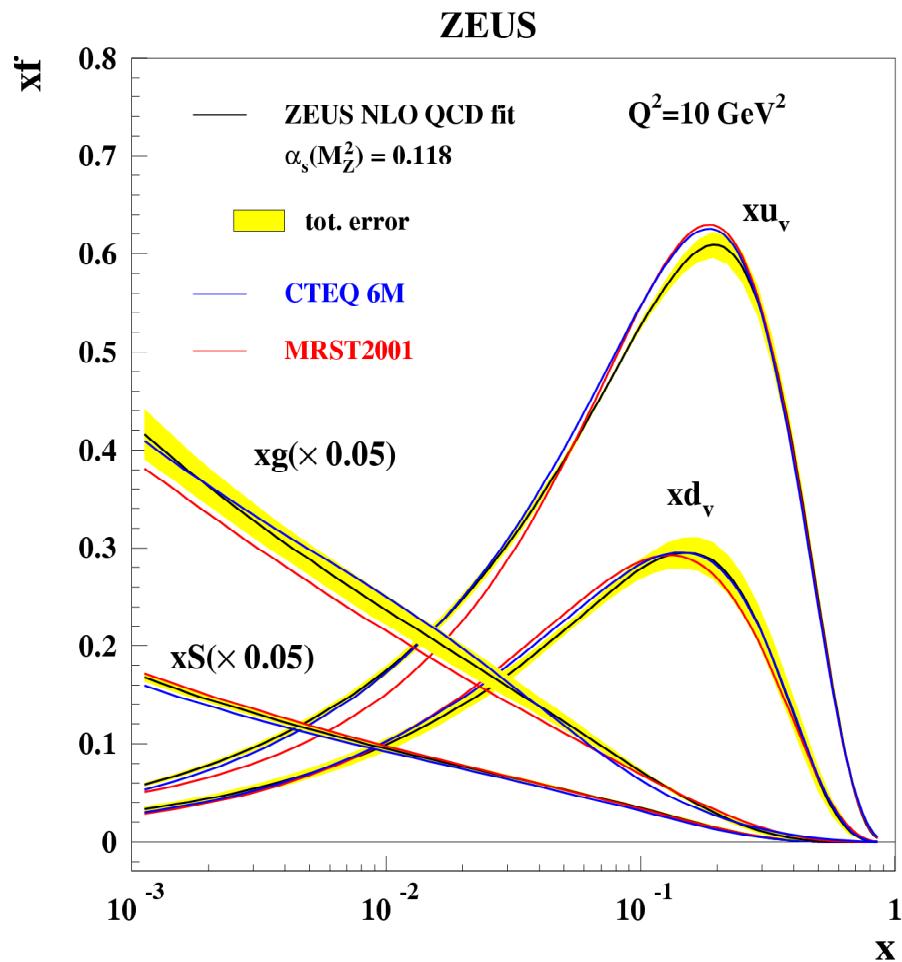
Testing QCD at small Bjorken x

# Hydrodynamics and inputs

- Initial condition:
  - thermalization time
  - energy density
  - (flow profile)
- Equation of state:
  - lattice QCD
- freezeout:
  - Hadron cascade after burner
  - (hadronic dissipative effects)
- Dissipative effects

Purpose: test uncertainties of the initial conditions.

# Gluon density



Gluon density dominates  $F_2$  for  $x < 0.01$

# Gauge field in the MV model

The gluon distribution is large:

**Suggest the use of the semi-classical methods**

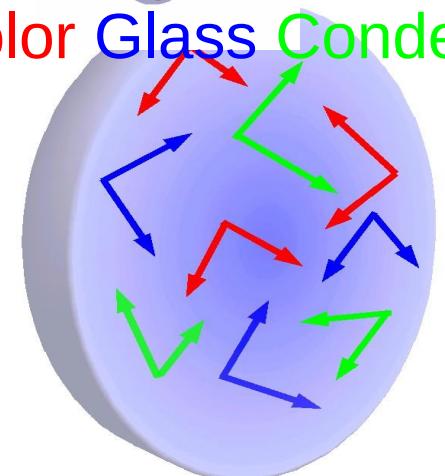
$$D_\nu F^{\nu\mu} = J^\mu$$

In the light-cone gauge:  $A^+ = 0$ ,  
a solution can be

$$A^- = 0, \quad A^i = \frac{i}{g} U \partial^i U^\dagger,$$
$$U = P \exp \left[ ig \int \Lambda dz^- \right], \quad -\Delta_\perp \Lambda = \rho$$

$\Lambda = A^+$   
in covariant  
gauge

Color Glass Condensate



transverse component:

gauge transformation of vacuum :  $F^{ij} = 0$

The only non-zero component of the field strength:  $F^{+i} \neq 0$

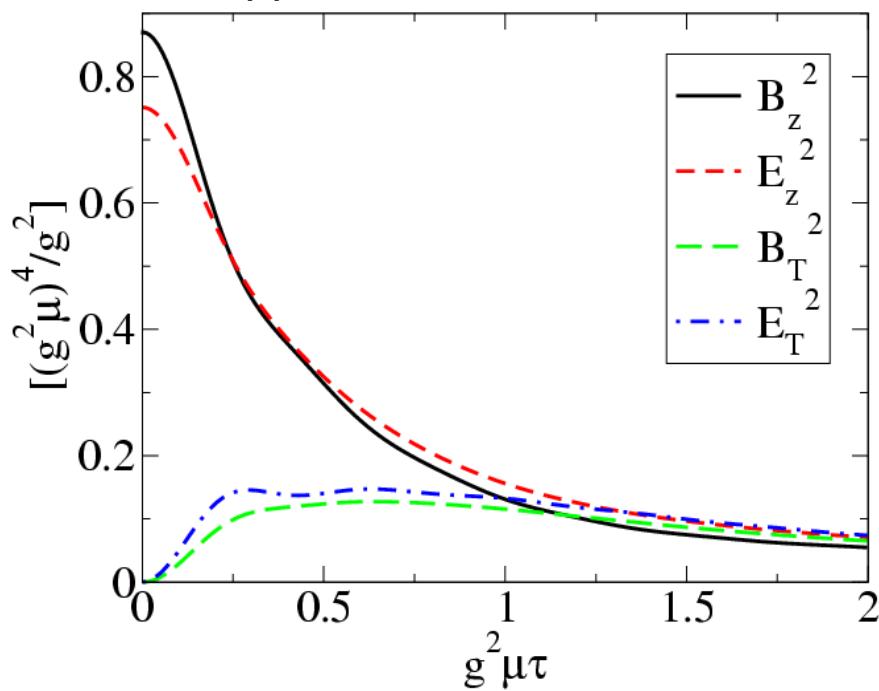
$$\mathbf{B} \cdot \mathbf{E} = 0, \quad B_z = E_z = 0$$

Non-abelian Weiszacker-Williams field

# $\tau < 1/Q_S$ : Yang-Mills field dynamics

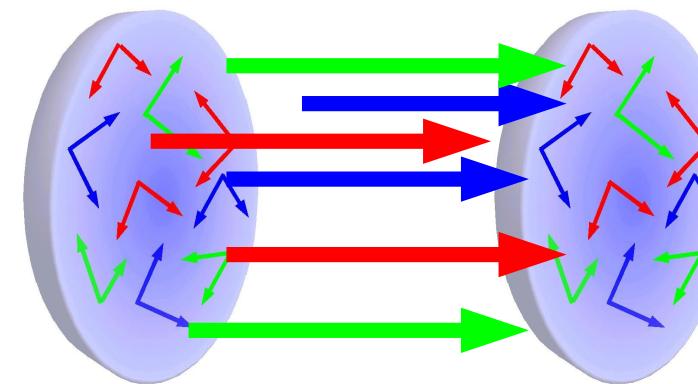
Real time evolution of the Classical Yang-Mills

T.Lappi, L. McLerran, N.P.A772



Similar to Lund string model picture:  
but produce both  
color electric  
and magnetic fields.

Production of longitudinal color EM fields.



Non-abelian Weiszacker-Williams filed

Non-abelian Weiszacker-Williams filed

Instabilities of Yang-Mills field :

P.Romatschke, R.Venugopalan,K.Fukushima, Gelis, McLerran, A.Iwazaki

# Gluon production based on CGC

- **x-evolution + Solving classical Yang-Mills equation**

CYM + IP-sat model, Schenke, Tribedy, Venugopalan

CYM+JIMWLK evolution, Lappi, Phys.Lett.B703(2011)325

- **rcBK evolution + kt-factorization formula**

$$\frac{dN_g}{d^2x_t dy} = \frac{4\pi N_c}{N_c^2 - 1} \int \frac{d^2 p_t}{p_t^2} \int d^2 k_t \alpha_s \varphi(x_1, k_t^2) \varphi(x_2, (p_t - k_t)^2)$$

Albacete, Armesto, Mihano, Salgado 2009 for HERA fit

Forward particle production: Dumitru Hayashigaki Jalilian-Marian (DHJ)

$$\frac{dN}{dy_h d^2 p_\perp} = \frac{K}{(2\pi)^2} \sum_{i=q,g} \int_{x_F}^1 x_1 f_{i/p}(x_1, p_\perp^2) N_i(x_2, p_\perp/z) D_{h/i(z, p_\perp)}$$

# Rapidity evolution

running coupling Balitsky-Kovchegov (rcBK) evolution

$$\frac{\partial \mathcal{N}(r, x)}{\partial y} = \int d^2 r_1 \ K(r, r_1, r_2) [\mathcal{N}(r_1, y) + \mathcal{N}(r_2, y) - \mathcal{N}(r, y) - \mathcal{N}(r_1, y) \mathcal{N}(r_2, y)]$$

$$y = \ln(x_0/x)$$

$$Q_s^2 \sim x^{-\lambda_{LO}}, \text{ with } \lambda_{LO} \simeq 4.88 N_c \alpha_s / \pi$$

$$K^{\text{LO}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) = \frac{N_c \alpha_s}{2\pi^2} \frac{r^2}{r_1^2 r_2^2}$$

HERA fit yields  $\lambda \sim 0.2 - 0.3$

LO-BK shows too fast evolution to fit HERA data.

$$K^{\text{run}}(\mathbf{r}, \mathbf{r}_1, \mathbf{r}_2) = \frac{N_c \alpha_s(r^2)}{2\pi^2} \left[ \frac{r^2}{r_1^2 r_2^2} + \frac{1}{r_1^2} \left( \frac{\alpha_s(r_1^2)}{\alpha_s(r_2^2)} - 1 \right) + \frac{1}{r_2^2} \left( \frac{\alpha_s(r_2^2)}{\alpha_s(r_1^2)} - 1 \right) \right]$$

Running of the coupling reduces the evolution speed down to values compatible with data (JLA PRL 99 262301 (07))

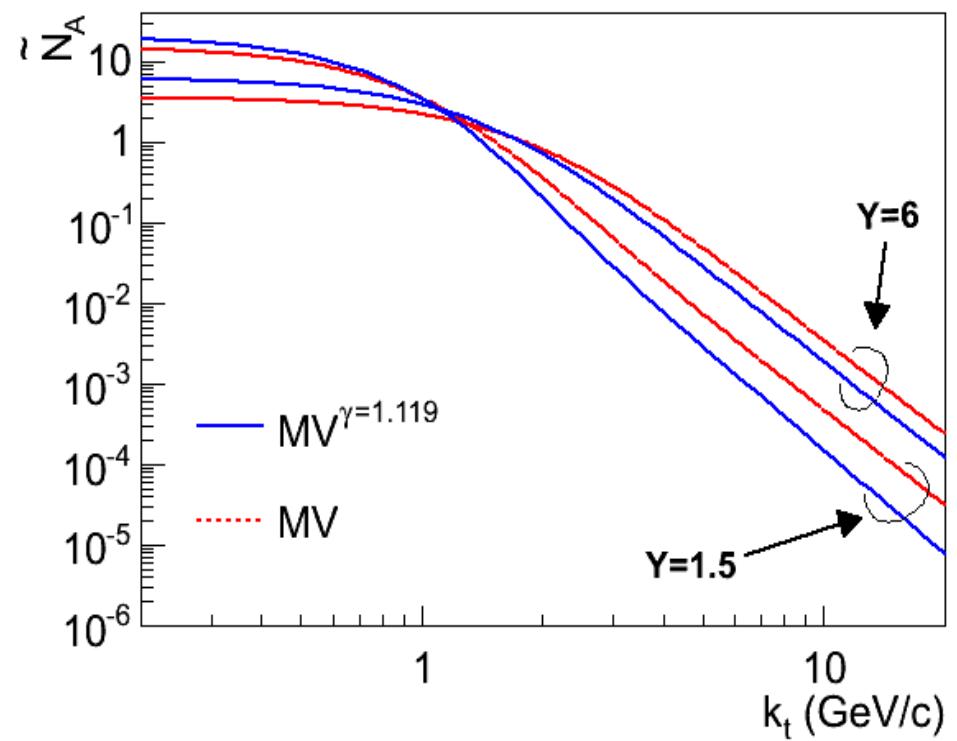
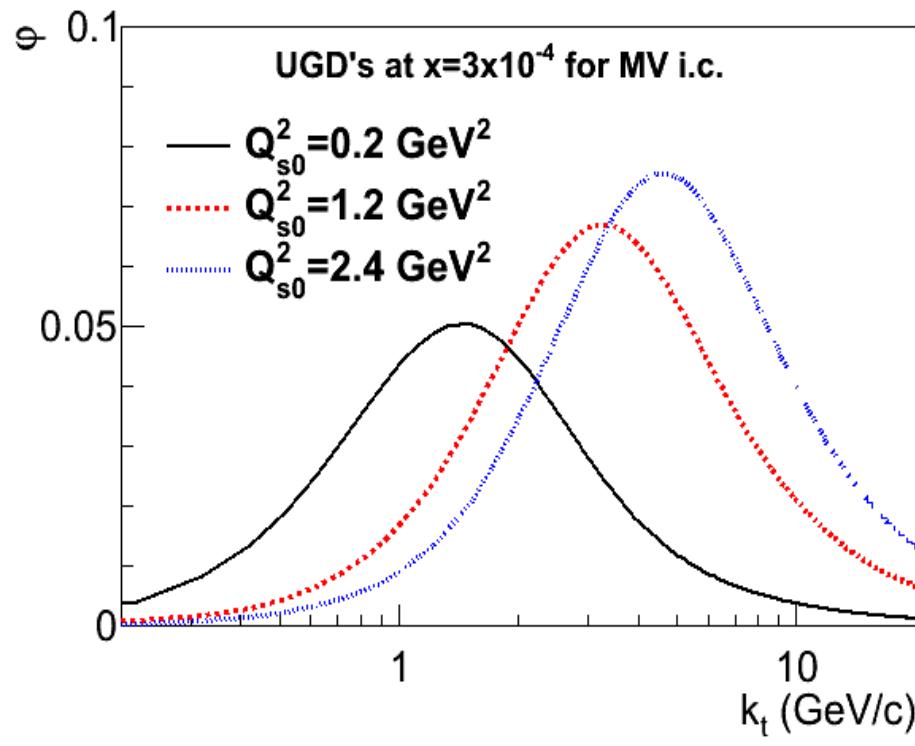
$$\mathcal{N}(r, x=x_0) = 1 - \exp \left[ -\frac{(r^2 Q_{s0}^2)^\gamma}{4} \ln \left( \frac{1}{r \Lambda} + e \right) \right]$$

# Unintegrated gluon distribution

$$\mathcal{N}(r, Y=0) = 1 - \exp \left[ -\frac{(r^2 Q_{s0}^2)^\gamma}{4} \ln \left( \frac{1}{\Lambda r} + e \right) \right] \quad \begin{aligned} \gamma &= 1.119 \\ Q_{s0}^2 &= 0.168 \text{ GeV}^2 \end{aligned}$$

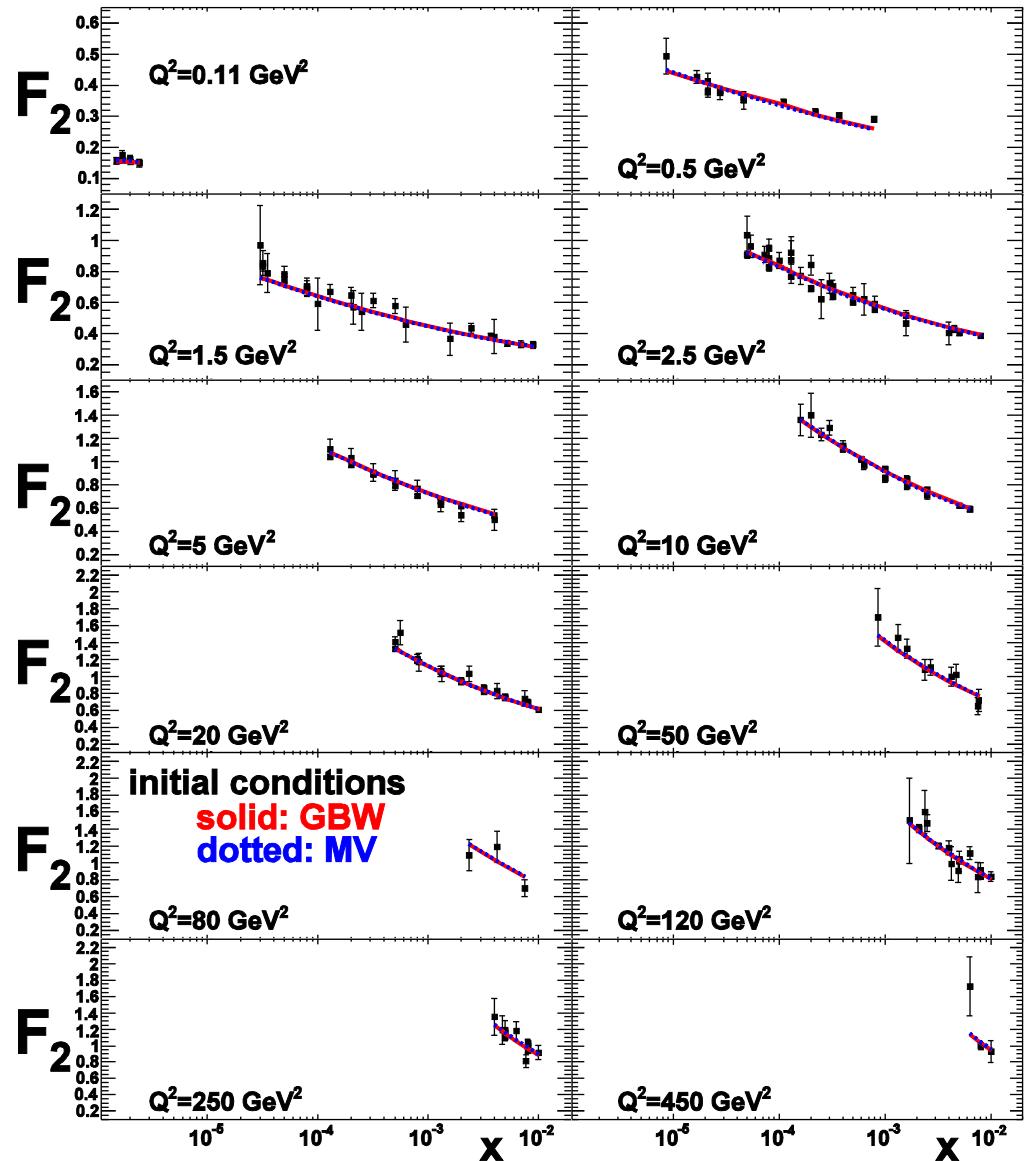
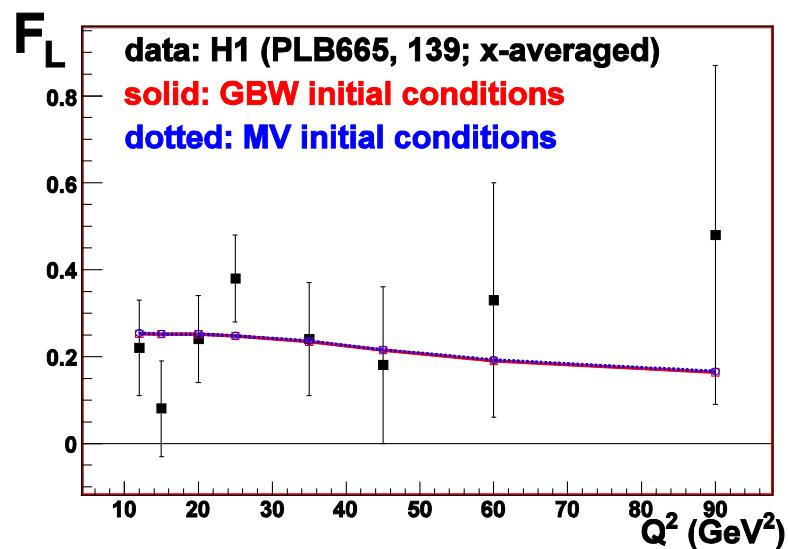
$$\varphi(k, x, b) = \frac{C_F}{\alpha_s(k) (2\pi)^3} \int d^2\mathbf{r} \ e^{-i\mathbf{k}\cdot\mathbf{r}} \nabla_{\mathbf{r}}^2 \mathcal{N}_G(r, Y=\ln(x_0/x), b)$$

MV i.c.:  $\gamma = 1$ ,  $Q_{s0}^2 = 0.2 \text{ GeV}^2$

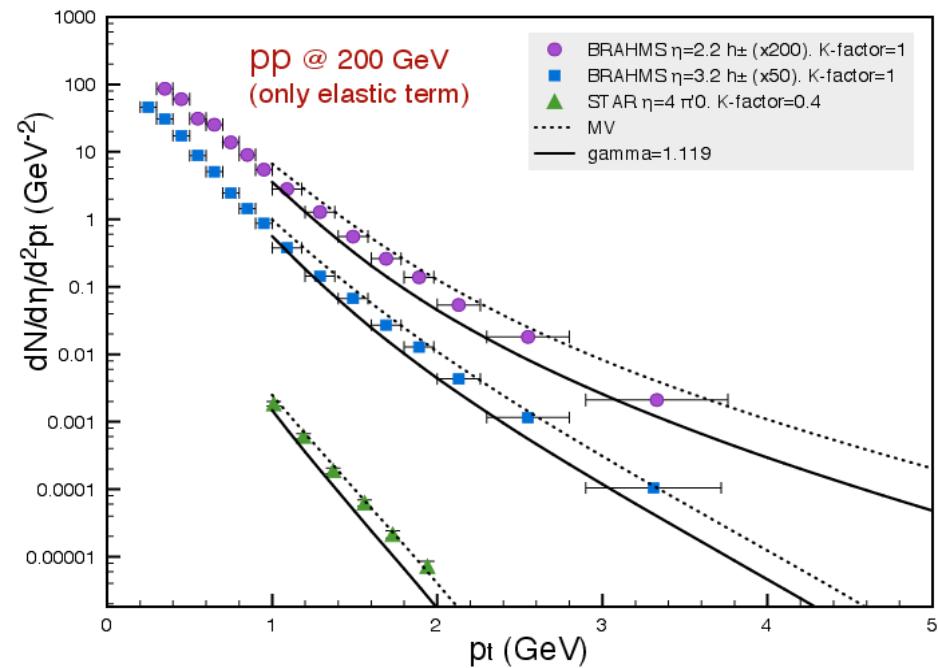


# HERA F2 data global fit from rcBK equation

Albacete, Armesto,  
Mihano, Salgado 2009

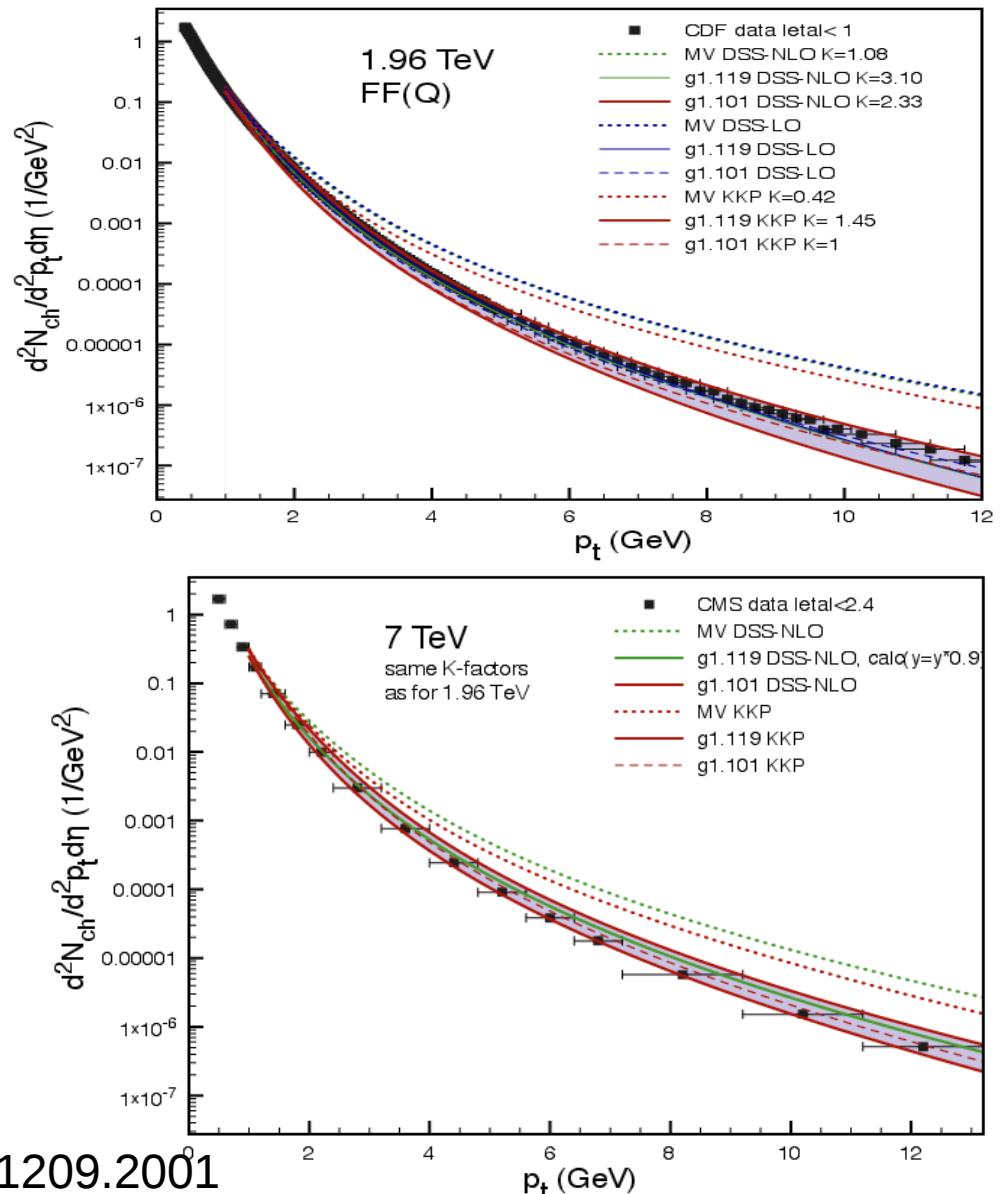


# Comparison to RHIC/LHC data for pp collisions



Strong constraint to  
the initial condition at LHC

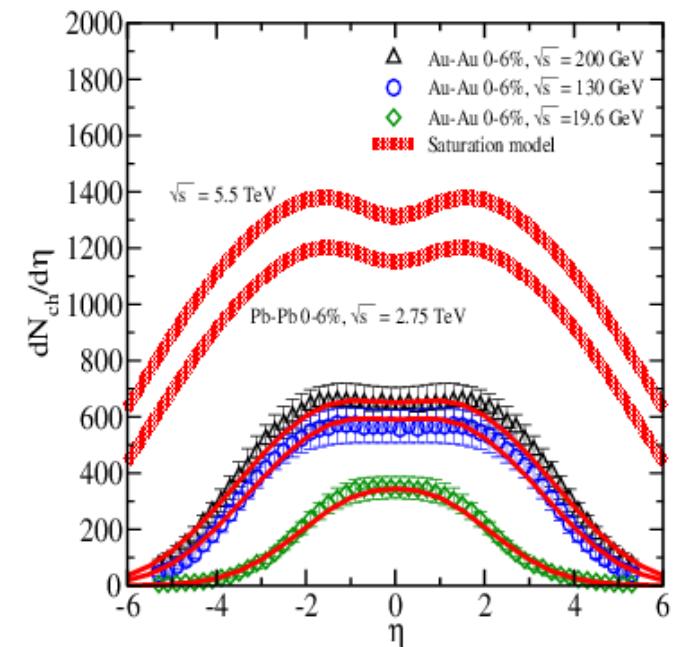
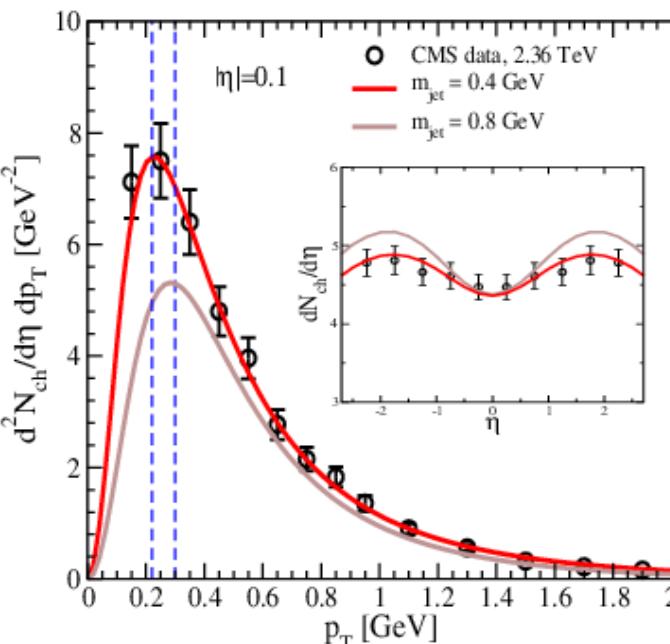
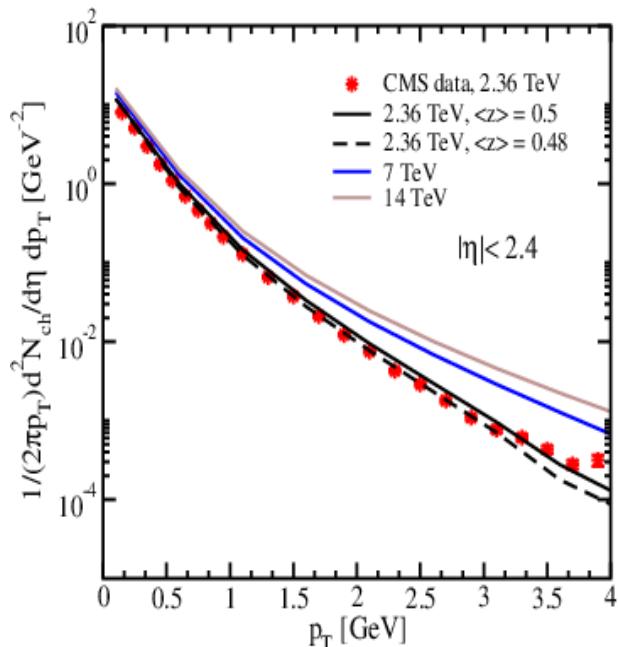
$\gamma > 1 \rightarrow$  evolution slow down



# Local parton-hadron duality

## Kt-factorization + LPHD

E.Levin and A. H.Rezaeian, Phys. Rev. D82,(2010)014022, Phys.Rev. D82 (2010) 054003



$$\frac{d\sigma}{dy} \frac{d^2}{dp_T^2} = -\frac{2\alpha_s}{C_F} \frac{1}{p_T^2} \int d^2 \vec{k}_T \, \phi(x_1; \vec{k}_T) \phi(x_2; \vec{p}_T - \vec{k}_T),$$

$$p_{j\cdot T, T} = \frac{p_T}{\langle z \rangle}, \quad \langle z \rangle = 0.5 \quad \vec{p}_T \rightarrow \sqrt{\vec{p}_T^2 + m_{jet}^2}$$

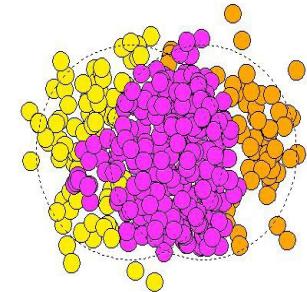
## Development of the model

- KLN model (2001): analytic expression for  $dN/dy$
- KLN + hydrodynamics (2004)
- fKLN (2006)
- MC-KLN (2007)
- MC-kt/rcBK and MC-DHJ/rcBK (2012)
- MC-Event Generator version of DHJ (2014)

# Monte-Carlo implementation

- Sample A and B nucleons according to the Woods-Saxon distribution.
- Collision: NN collision probability  $P(b) = 1 - \exp[-kT_{pp}(b)]$   
 $T_{pp}(b) = \int d^2s T_p(s) T_p(s - b)$        $(x_i - x_j)^2 + (y_i - y_j)^2 \leq \frac{\sigma_{NN}}{\pi}$   
 $k$  is fixed by the relation  $\sigma_{in} = \int d^2b (1 - \exp[-kT_{pp}(b)])$
- Local density of nucleons at each grid is obtained by

$$T_p(r) = \frac{1}{2\pi B} \exp[-r^2/(2B)]$$



- which is used to simulate coherent scattering
- For each generated configuration, we apply the k\_t-factorization formula at each transverse grid.

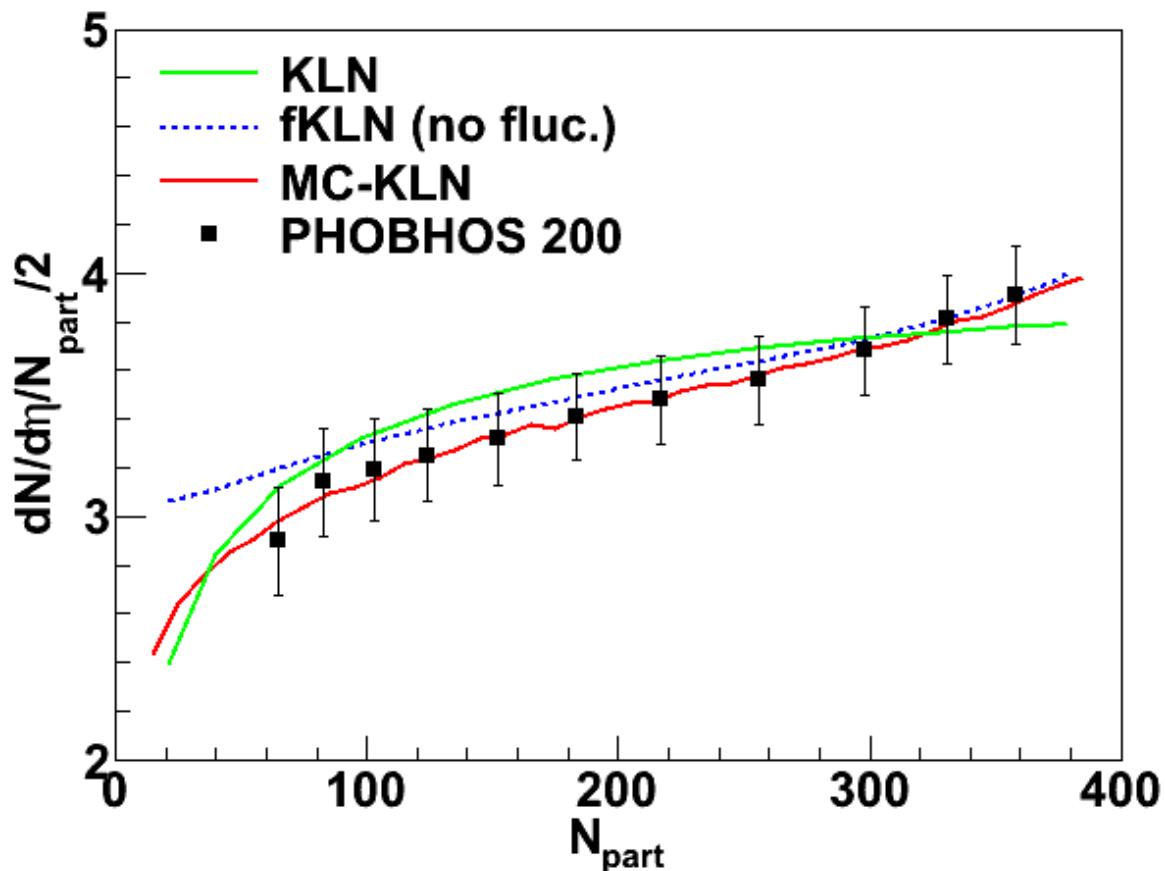
$$\frac{dN_g}{d^2x_t dy} = \frac{4\pi N_c}{N_c^2 - 1} \int \frac{d^2p_t}{p_t^2} \int d^2k_t \alpha_s \varphi(x_1, k_t^2) \varphi(x_2, (p_t - k_t)^2)$$

$$\varphi(k, x, b) = \frac{C_F}{\alpha_s(k) (2\pi)^3} \int d^2\mathbf{r} e^{-i\mathbf{k}\cdot\mathbf{r}} \nabla_{\mathbf{r}}^2 \mathcal{N}_G(r, Y = \ln(x_0/x), b)$$

implemented by A.Dumitru by using the solution of rcBK from J. L. Albacete.

[http://physics.baruch.cuny.edu/node/people/adumitru/res\\_cgc](http://physics.baruch.cuny.edu/node/people/adumitru/res_cgc)

# Centrality dependence at $y=0$



$$\frac{1}{N_{\text{part}}} \frac{dN}{dy} = c \ln \left( \frac{Q_s^2}{\Lambda_{\text{QCD}}^2} \right)$$

The effect of fluctuation is seen in the peripheral collisions ( $N_{\text{part}} < 200$ ).

# Initial transverse geometry for hydro initial conditions

Glauber model

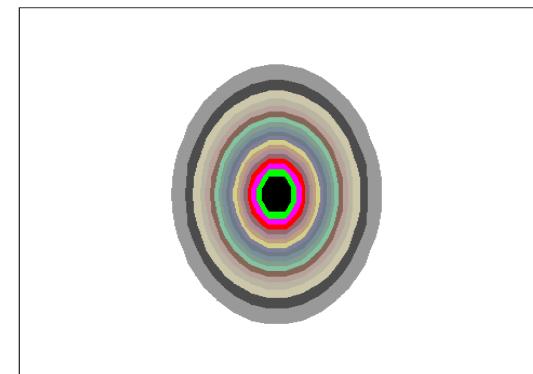
$$\frac{dN}{d^2 \mathbf{x}_\perp dy} \sim N_{part,1}(\mathbf{x}_\perp) + N_{part,2}(\mathbf{x}_\perp)$$

CGC

$$\frac{dN}{d^2 \mathbf{x}_\perp dy} \sim \min \{ N_{part,1}(\mathbf{x}_\perp), N_{part,2}(\mathbf{x}_\perp) \}$$

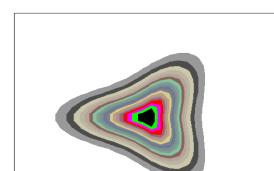
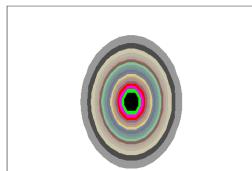
$$\varepsilon = \frac{\langle y^2 - x^2 \rangle}{\langle x^2 + y^2 \rangle}$$

$$\varepsilon_{CGC} > \varepsilon_{Glauber}$$

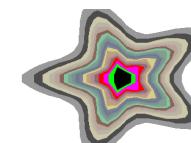
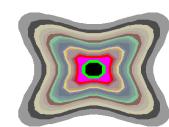
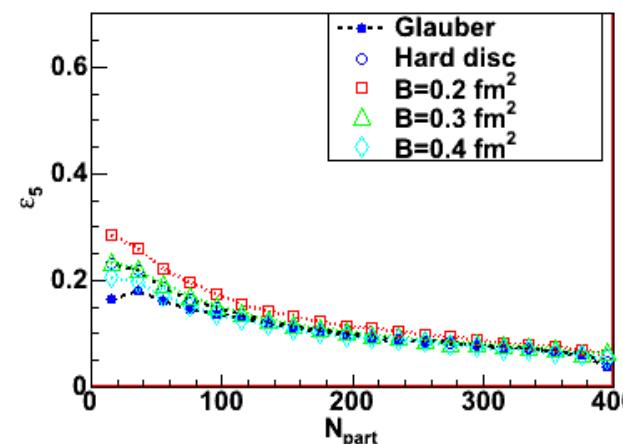
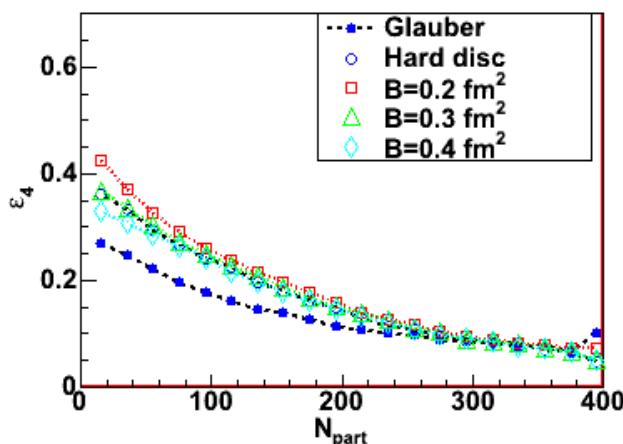
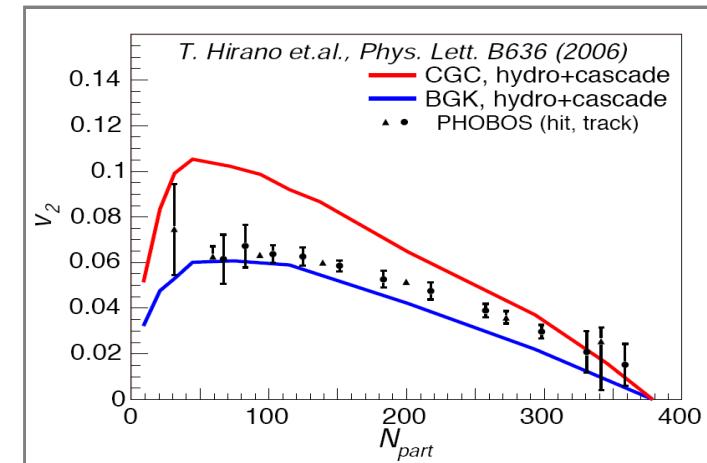
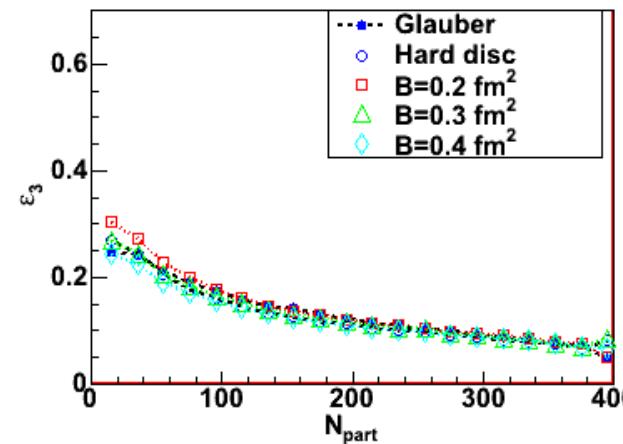
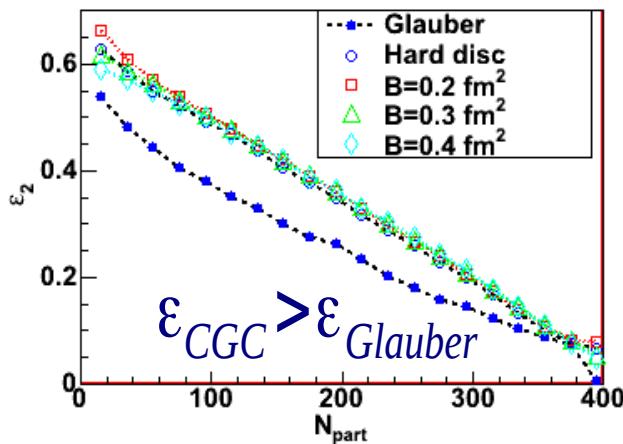


$$\varepsilon = \frac{\langle y^2 - x^2 \rangle}{\langle x^2 + y^2 \rangle}$$

# Large v2 in CGC



$$\epsilon_n = \frac{\sqrt{\langle r^2 \cos(n\phi) \rangle^2 + \langle r^2 \sin(n\phi) \rangle^2}}{\langle r^2 \rangle}$$



$$v_2 \equiv \langle \cos(2\phi) \rangle = \left\langle \frac{p_x^2 - p_y^2}{p_x^2 + p_y^2} \right\rangle$$

# Monte-Carlo event generator for CGC

First attempt: BBL (Black-Body limit) Monte-Carlo Model  
based on kt-factorization and SIBYLL

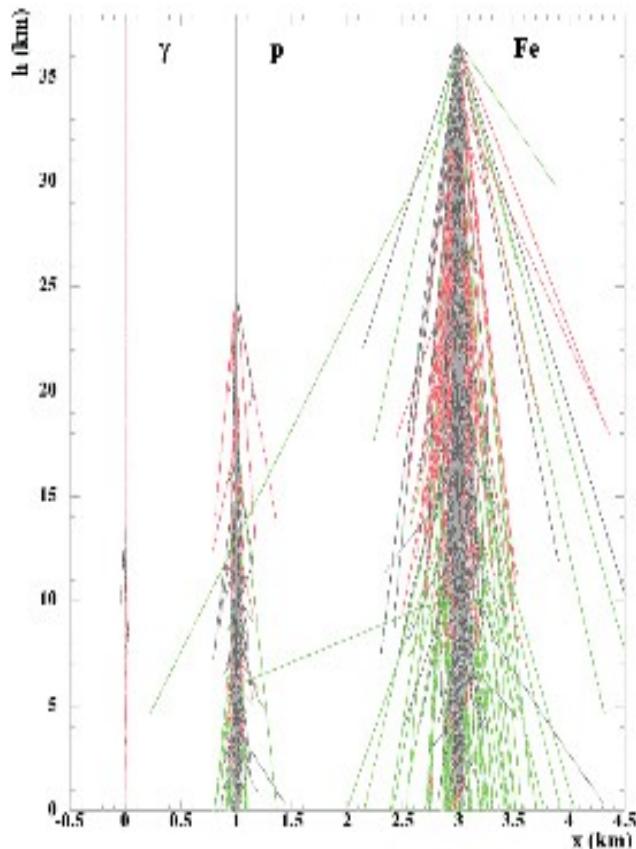
by

H.J. Drescher, A. Dumitru, M. Strikman, Phys.Rev.Lett. 94 (2005) 2

We would like to develop generator based on

DHJ (Dumitru-Hayashigaki-Jalilian-Marian) formula with rcBK unintegrated gluon dist.  
for the description of forward hadron productions.

# High energy cosmic rays and extensive air showers



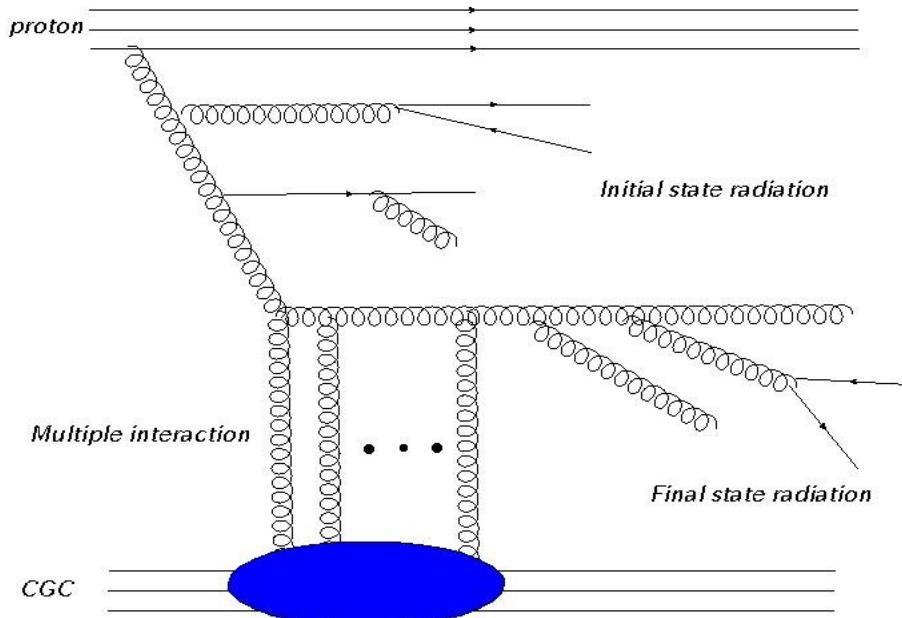
Air showers are initiated by extremely energetic primary cosmic ray hadrons

$$E > 10^{13} \text{ eV} \text{ or } > 10 \text{ TeV}$$

Largest systematic uncertainty in the analysis of air shower is caused by the uncertainty of hadronic interaction of cosmic ray in atmosphere.

# Monte-Carlo Event Generator for DHJ approach

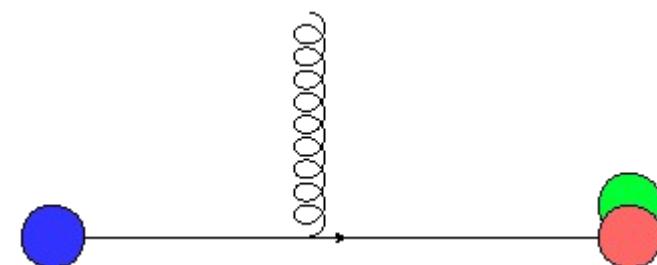
$gg \rightarrow g, gq \rightarrow q$  with initial and final state radiations



Gluons and quarks are generated according to the DHJ formula.

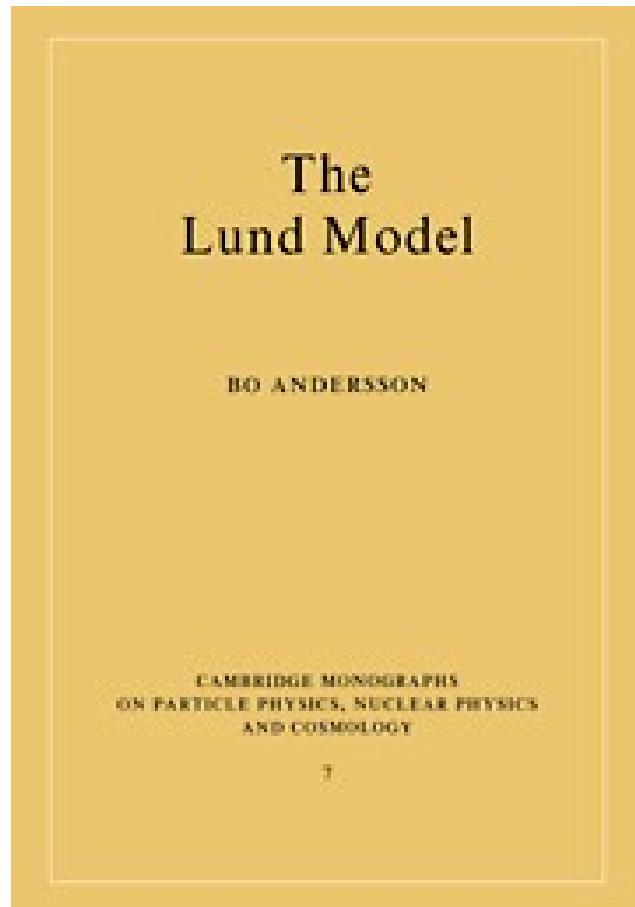
$$\frac{dN}{dy d^2 p_\perp} = \frac{K}{(2\pi)^2} f_{i/p}(x_1, p_\perp^2) N_i(x_2, p_\perp^2)$$

Hadrons are produced by the Lund string fragmentation model



# Lund model

<http://home.hep.lu.se/~torbjorn/Pythia.html>



B. Andersson, G. Gustafson, G. Ingelman and T. Sjostrand,  
"Parton Fragmentation And String Dynamics,"  
*Phys. Rept.* 97, 31 (1983).

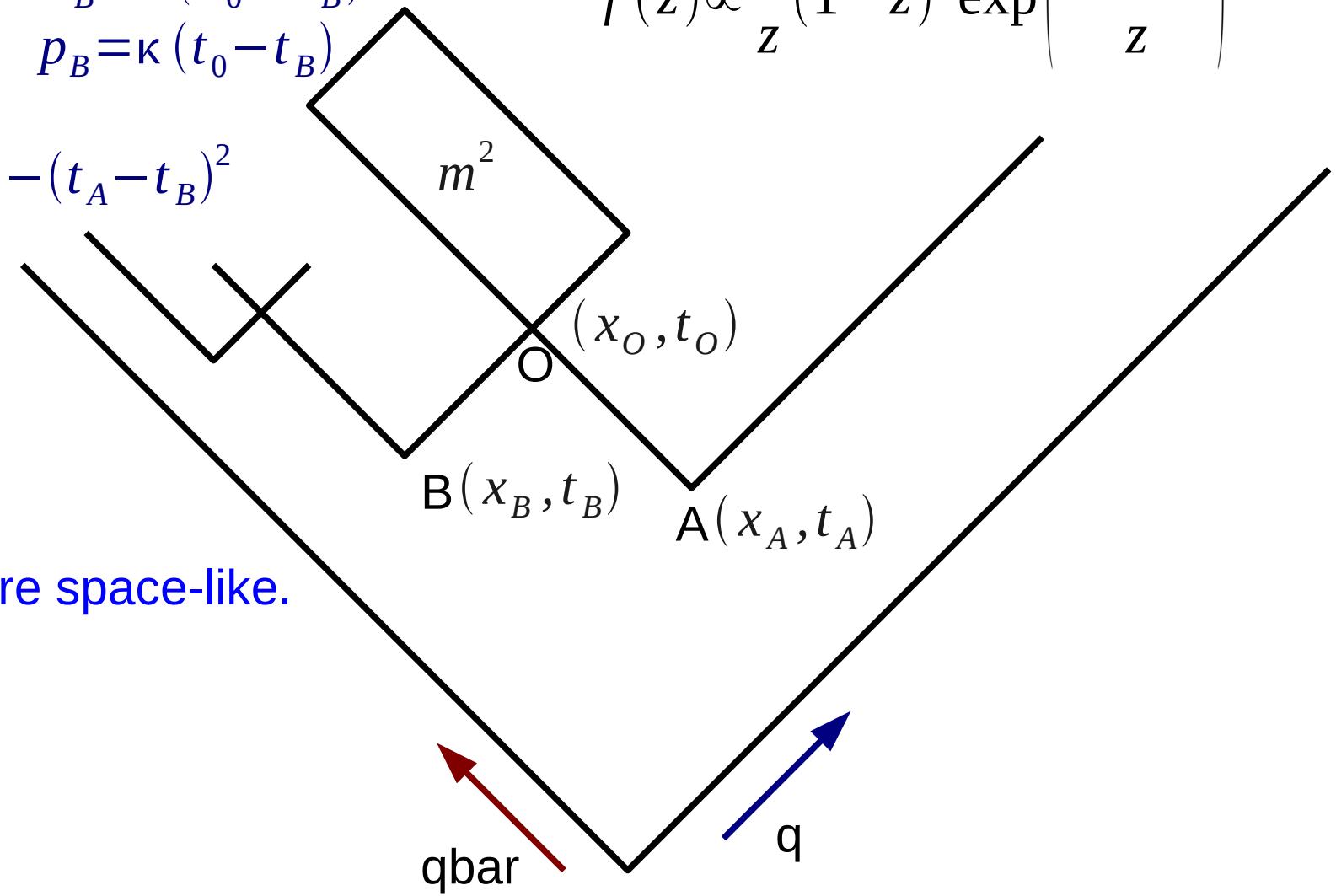
PYTHIA6.4 Physics and Manual 489pages

# String breaking

$$E_A = \kappa(x_A - x_0), \quad E_B = \kappa(x_0 - x_B)$$
$$p_A = \kappa(t_A - t_0), \quad p_B = \kappa(t_0 - t_B)$$

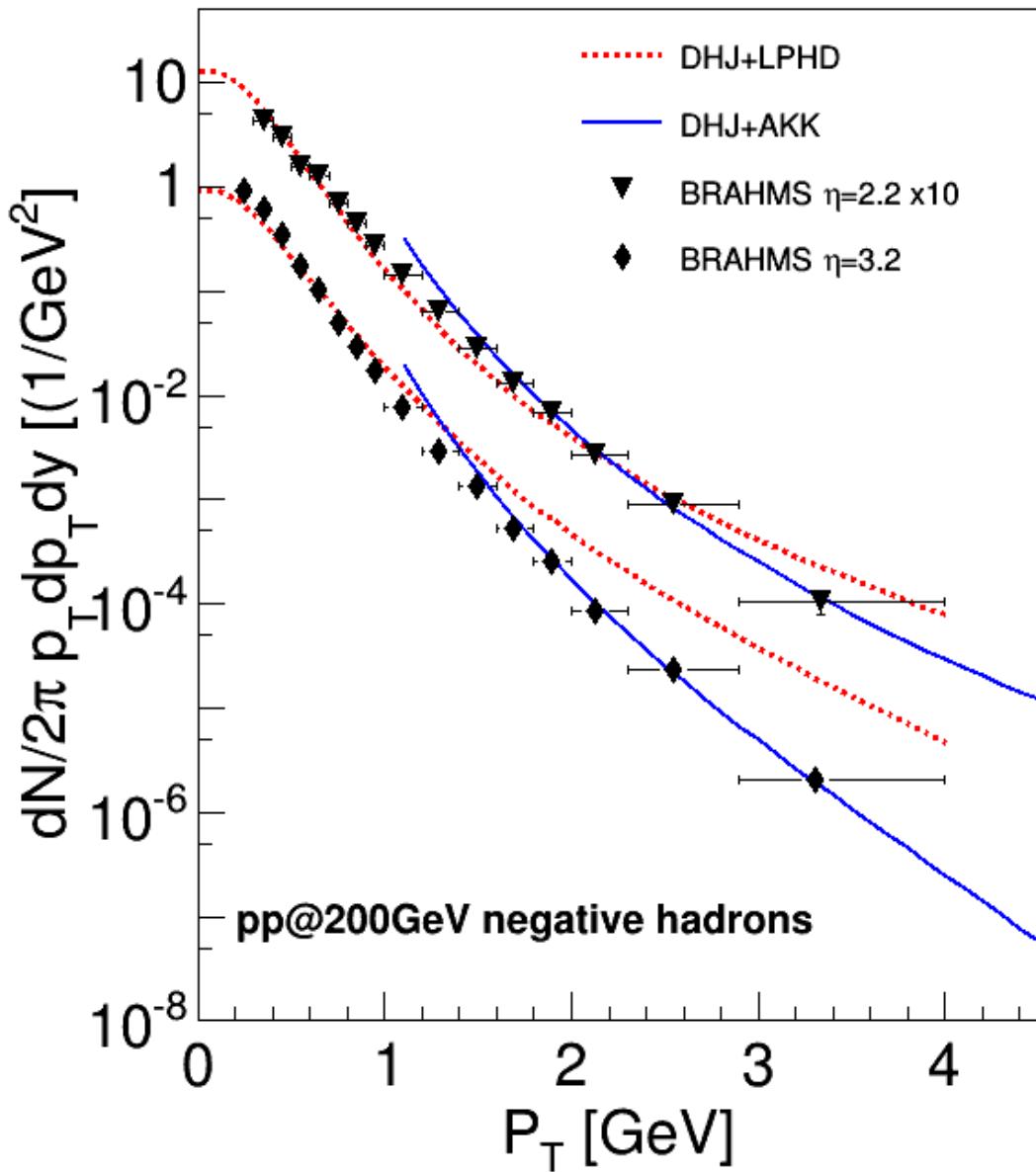
$$\frac{m^2}{\kappa^2} = (x_A - x_B)^2 - (t_A - t_B)^2$$

$$f(z) \propto \frac{1}{z} (1-z)^a \exp\left(\frac{-bm_\perp^2}{z}\right)$$



Vertex A and B are space-like.

# LPHD and FF in DHJ

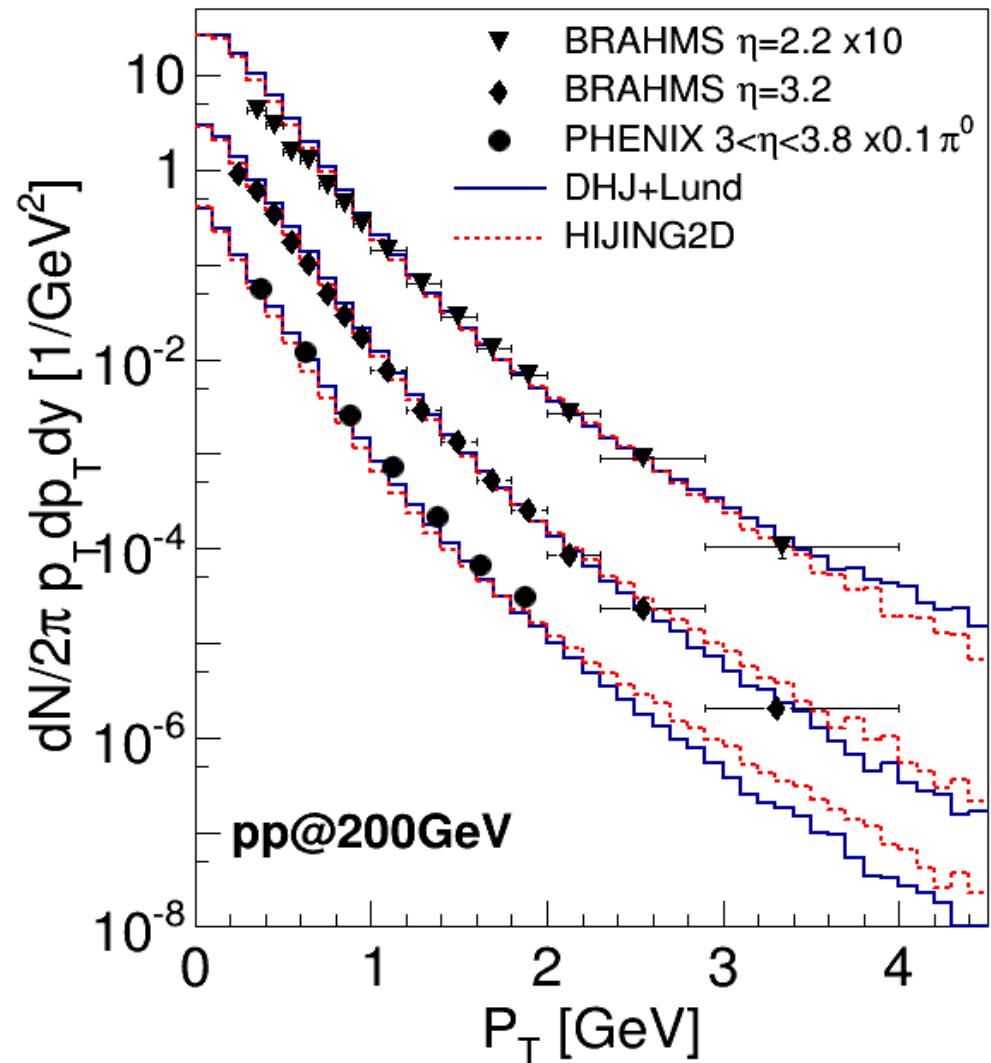
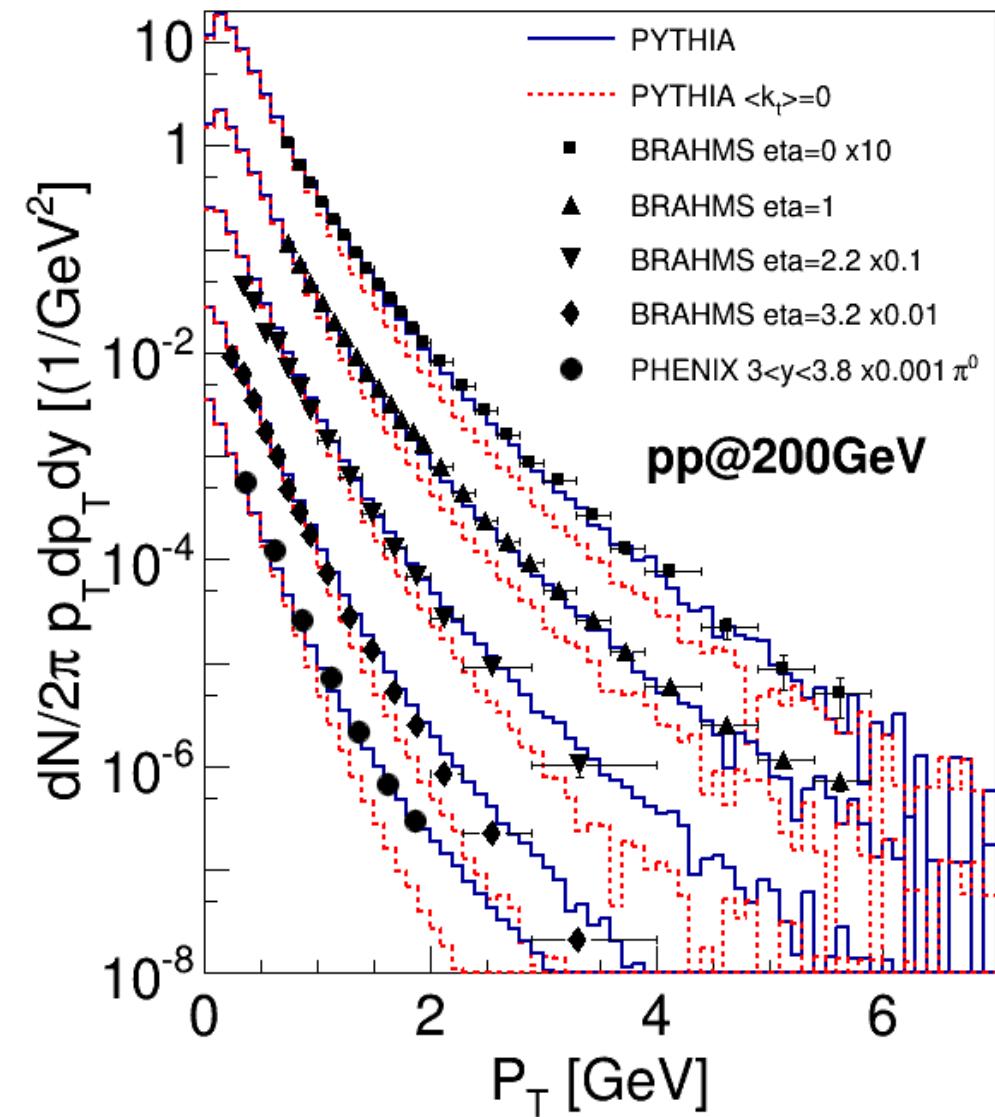


Within kt-factrizaton approach,  
High pt hadrons are well  
described by  
the [Fragmentation function](#),

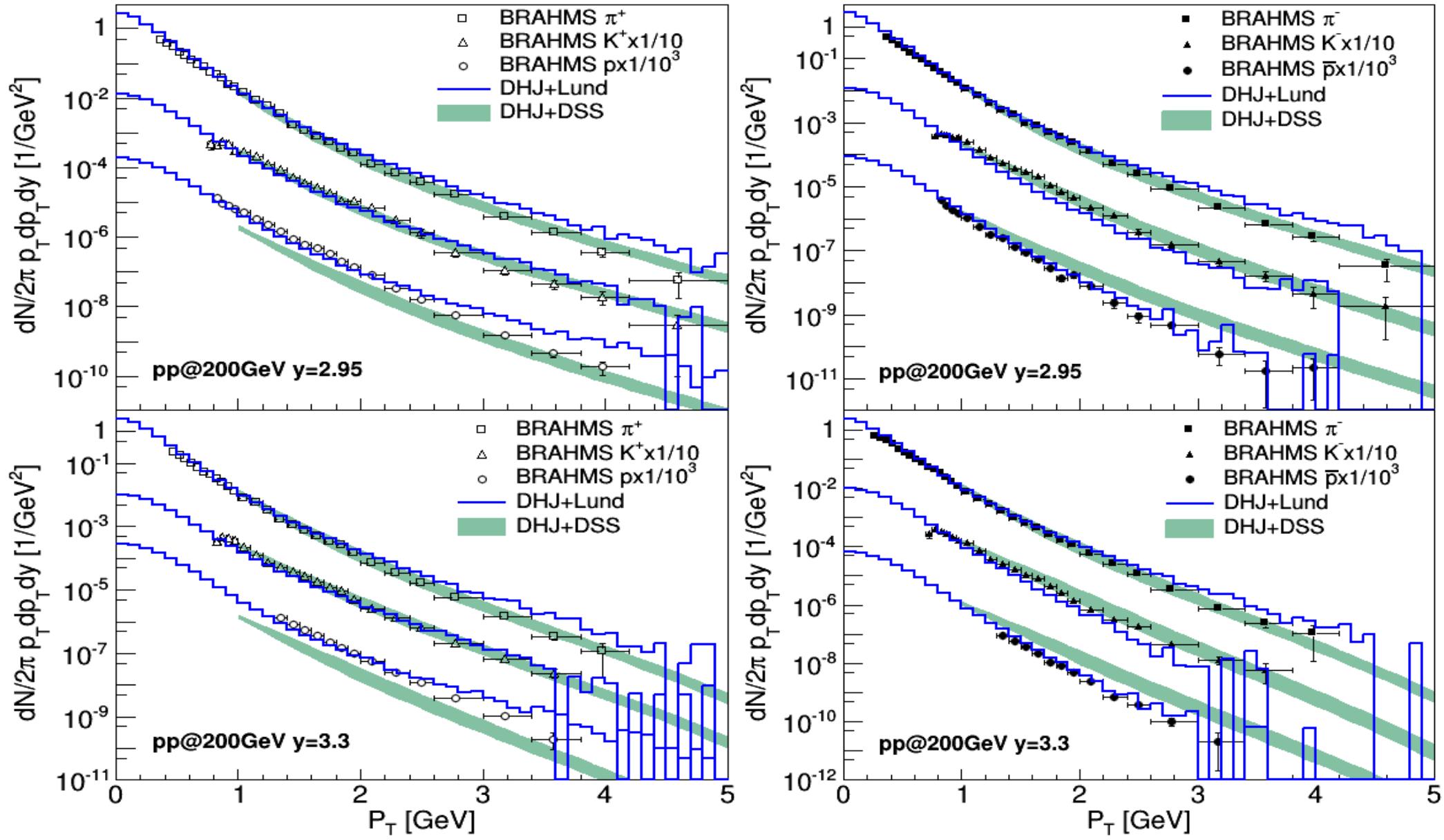
Low pt hadrons including  
multiplicity are well described  
by the [parton-padron duality](#).

More realistic model:  
event generator version is needed  
for the unified description..

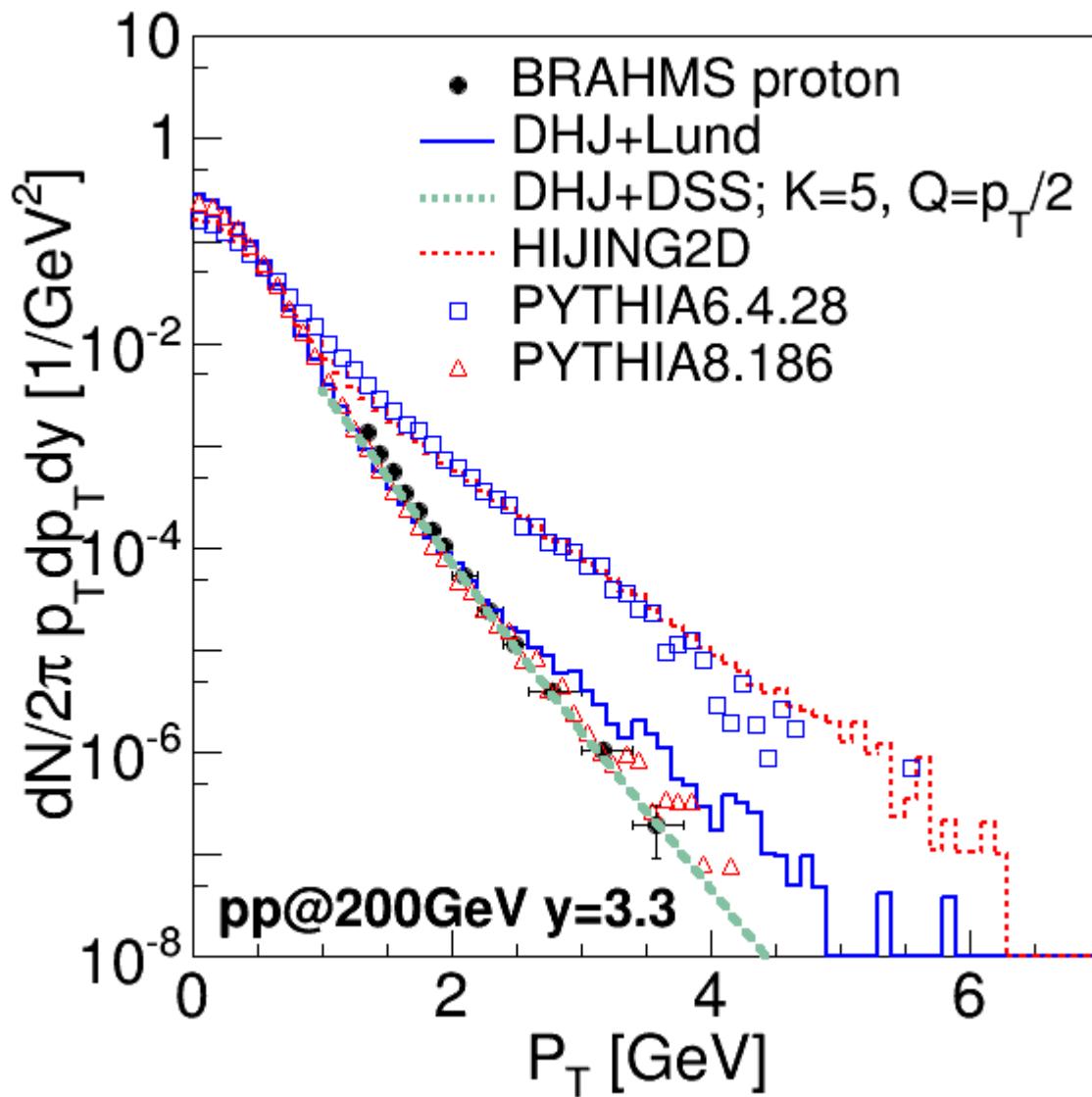
# P + P@200GeV negative hadrons



# Identified hadrons@200GeV

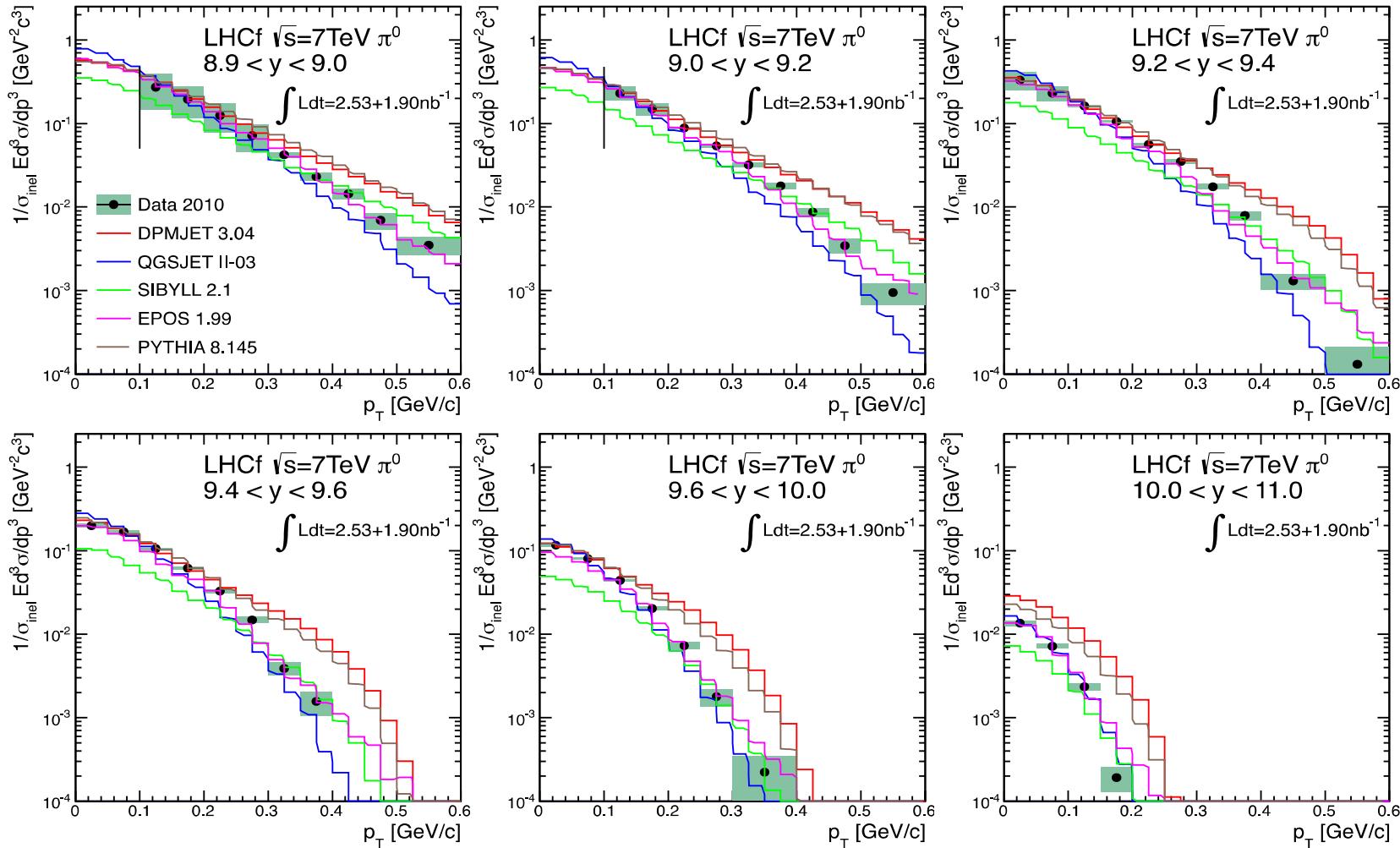


# Proton distribution at $y=3.3$



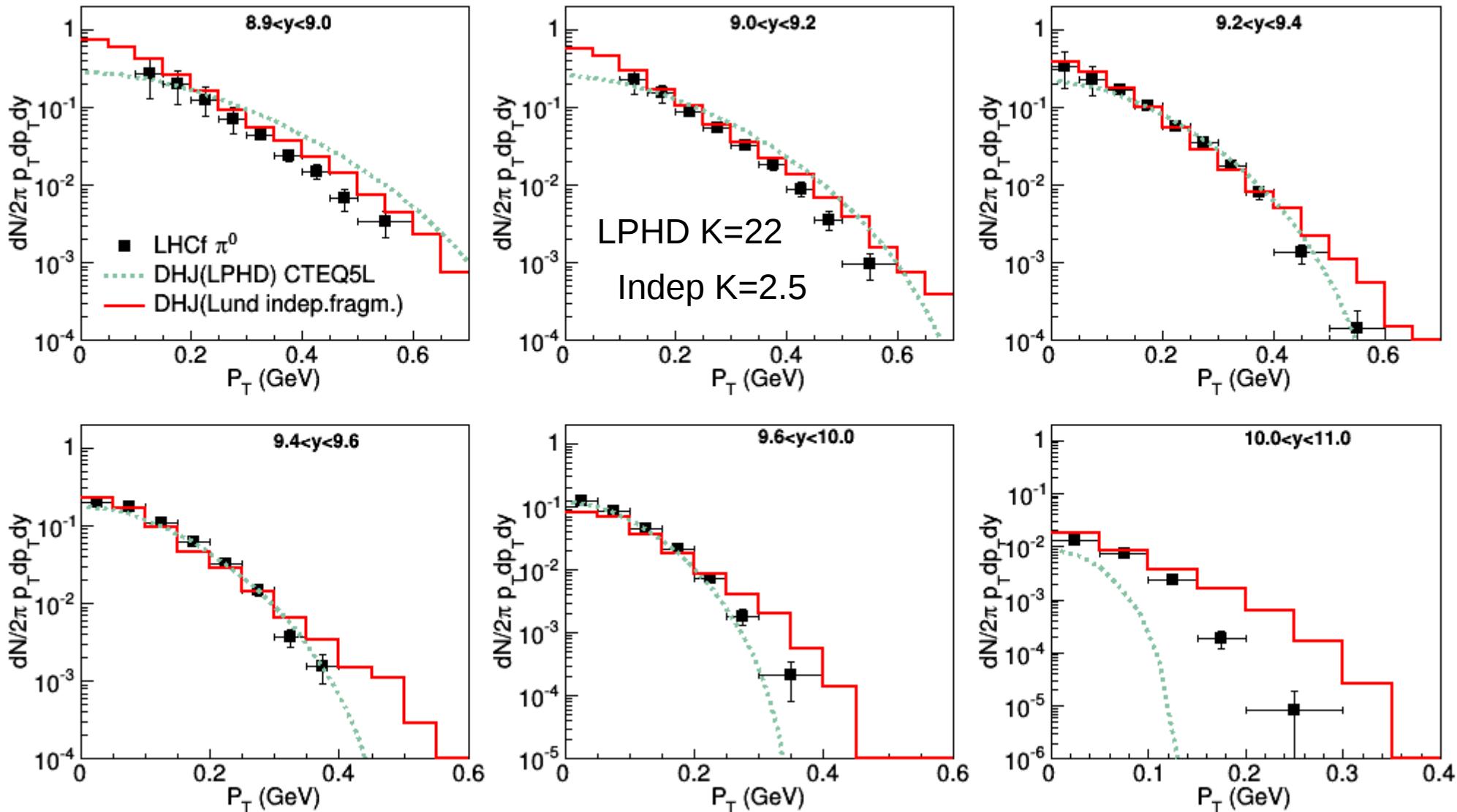
# Forward neutral pion from LHCf

$$x \approx 1 \times 10^{-7}$$

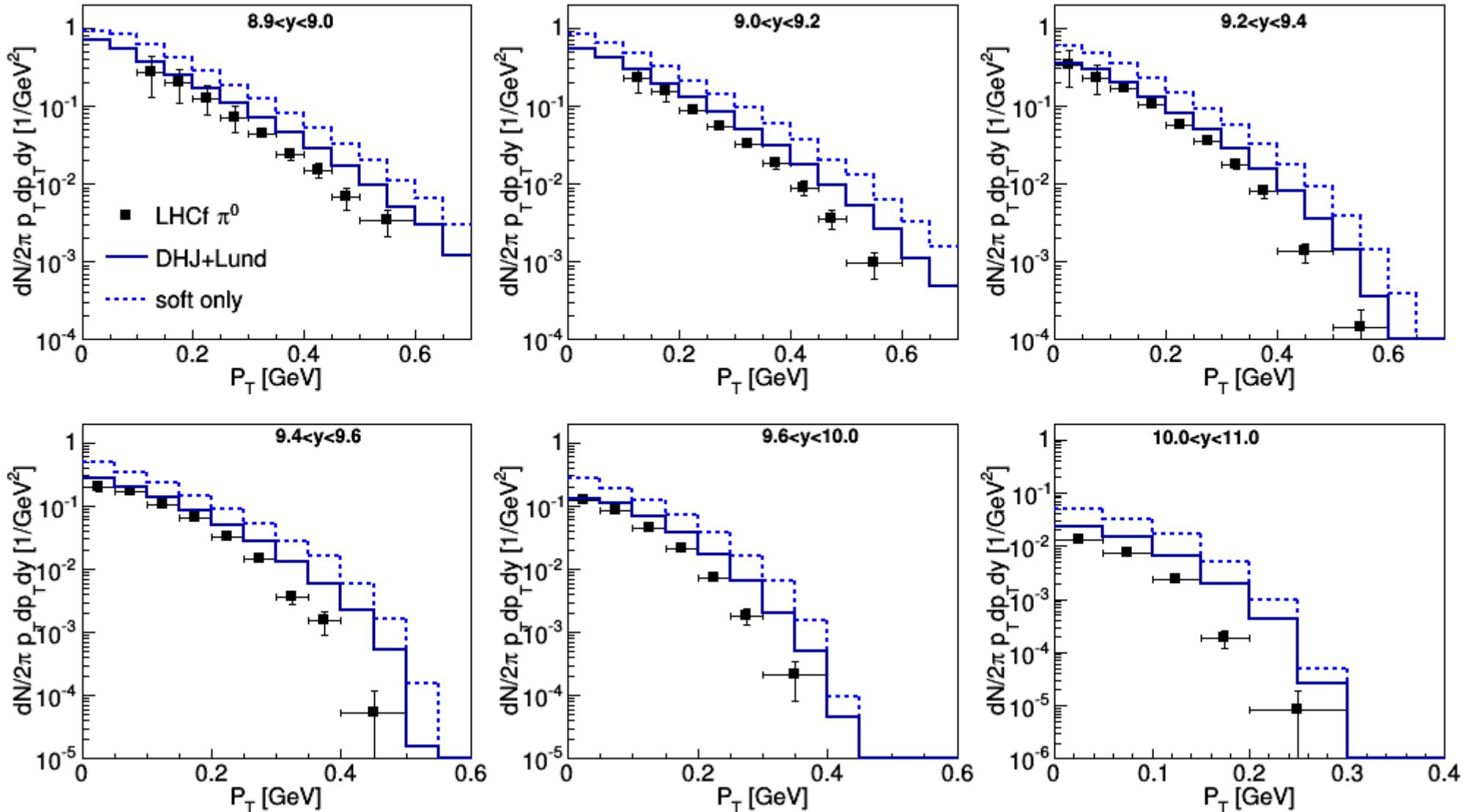


# Gluon contribution? LHCf pp@7TeV

$$\langle z \rangle = (1 + z_{\min})/2 \quad x \approx 1 \times 10^{-7}$$



# DHJ+Lund v.s. soft string fragm.py8



# summary

- Monte-Carlo Event Generator version of DHJ model has been newly developed.  
*DHJ + Lund string fragmentation model*
- We use unintegrated gluon function from rcBK equation which is fitted by HERA data at  $x < 0.01$ .
- Particle distribution for pp collisions are well fitted by the model from low to high momentum region.
  - Extension to pA and AA
  - Initial state radiation due to x-evolution